

Jack has been walking for  $12 \text{ min} \pm 3 \text{ min}$ . She has been walking at a speed of  $4 \text{ m/min} \pm 2 \text{ m/min}$ .

What is the uncertainty  $\Delta d$  in the distance he has traveled,  
 $d \pm \Delta d = (v \pm \Delta v)(t \pm \Delta t) = 48 \text{ m} \pm \Delta d$ ?

Note that  $(4 \text{ m/min})(12 \text{ min}) = 48 \text{ m}$ .

- A)  $\Delta d = 44 \text{ m}$
  - B)  $\Delta d = 36 \text{ m}$
  - C)  $\Delta d = 54 \text{ m}$
  - D)  $\Delta d = 48 \text{ m}$
  - E)  $\Delta d = 24 \text{ m}$
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$$\begin{aligned}d \pm \Delta d &= (v \pm \Delta v)(t \pm \Delta t), \quad \text{as given, so} \\ &= vt \left(1 \pm \frac{\Delta v}{v}\right) \left(1 \pm \frac{\Delta t}{t}\right) \\ &= d \pm (t \Delta v + v \Delta t + \Delta v \Delta t), \quad \text{which reduces to} \\ \Delta d &= t \Delta v + v \Delta t, \quad \text{since} \\ \Delta v \Delta t &\approx 0 \quad \text{in first order.}\end{aligned}$$

Using calculus notation, we have the same result

$$\begin{aligned}\Delta d &= \left| \frac{\partial d}{\partial v} \right| \Delta v + \left| \frac{\partial d}{\partial t} \right| \Delta t \\ &= |t| \Delta v + |v| \Delta t \\ &= (12 \text{ min})(2 \text{ m/min}) + (4 \text{ m/min})(3 \text{ min}) \\ &= (24 \text{ m}) + (12 \text{ m}) \\ &= \boxed{36 \text{ m}}, \quad \text{since} \\ \frac{\partial d}{\partial v} &= \frac{\partial}{\partial v} vt = t = 12 \text{ min}, \quad \text{and} \\ \frac{\partial d}{\partial t} &= \frac{\partial}{\partial t} vt = v = 4 \text{ m/min}.\end{aligned}$$

Answer **B**.