

Field- and current-driven domain wall dynamics: An experimental picture

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Abstract

Field- and current-driven domain wall velocities are measured and discussed in terms of existing spin-torque models. A reversal in the roles of adiabatic and non-adiabatic spin-torque is shown to arise in those models below and above Walker breakdown. The measured dependence of velocity on current is the same in both regimes, indicating both spin-torque components have similar magnitude. However, the models on which these conclusions are based have serious quantitative shortcomings in describing the observed field-driven wall dynamics, for which they were originally developed. Hence, the applicability of simple one-dimensional models to most experimental conditions may be limited.

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The capacity of a spin-polarized current to move a domain wall is experimentally well established [1–3], but the mechanisms responsible for that motion [4–9] remain under debate. Models fall into two classes, termed “adiabatic” [4–6] and “non-adiabatic” [5,7–9]. Most analytical work has cast these interactions within the framework of one-dimensional (1D) domain wall dynamics formulated decades ago [10]. Here we outline the predicted wall dynamics, present experimental characterizations of these dynamics, and discuss them in terms of the 1D models. Interpretation of the data within a 1D model framework provides estimates of relevant spin-torque parameters. However, the same model predicts key parameters of field-driven motion at odds with experiment by up to three orders of magnitude. The quantitative failure of the 1D model to describe field-driven motion warrants caution in directly extending the model to current-driven motion.

A wall geometry appropriate for most recent experiments [2,3] is shown in Fig. 1. The orientation of each spin

is denoted (θ, ϕ) , and $\theta(x)$ varies from 0 to π over a characteristic width Δ [10]. The wall is described by two collective coordinates derived from θ and ϕ : the wall displacement q and its canting angle ψ . Wall motion requires a torque on θ to bring the wall spins toward the applied field H_a . However, H_a applies a torque not to θ , but to ϕ , and thus cannot directly drive wall motion. Instead, H_a cants ψ away from the easy plane and a demagnetizing field H_d develops. It is the demagnetizing torque, $\gamma \vec{M} \times \vec{H}_d$, that drives θ and consequent wall motion \dot{q} . The existence of a velocity maximum [10] then follows naturally. At $\psi = \pi/4$, the demagnetizing torque, and thus \dot{q} , peaks. If H_a drives ψ past this limit, ψ can no longer remain

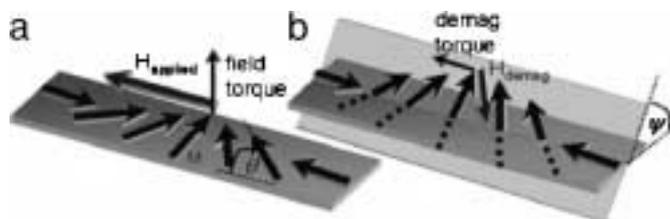


Fig. 1. Domain wall subjected to an axial field.

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stationary, a transition termed Walker breakdown. ψ advances continually and the demagnetizing torque contribution to $\dot{\mathbf{q}}$, $(\gamma\vec{M} \times \vec{H}_d)$, changes direction with each quarter period, averaging to zero. ψ rotation becomes more rapid with increasing H_a , leading to a small net damping torque $(\alpha\vec{M} \times \dot{\mathbf{M}})$ that cants the wall spins toward H_a and drives the wall forward. At high H_a , this damping torque provides the sole contribution to $\dot{\mathbf{q}}$.

In this picture, the roles of adiabatic and non-adiabatic spin-torque are, loosely, to drive ψ and \mathbf{q} motion, respectively, and the following equations of motion emerge [5,9]:

$$\dot{\mathbf{q}} = (2\pi\mathbf{M}_s)\gamma \Delta \sin 2\psi + \alpha \Delta \dot{\psi} + \eta \mathbf{u}, \quad (1a)$$

$$\dot{\psi} = \gamma H_a - (\alpha/\Delta)\dot{\mathbf{q}} + (\beta\mathbf{u})/\Delta. \quad (1b)$$

A current density \mathbf{j} is included via $\mathbf{u} = -(\mathbf{g}\mu_B\mathbf{p}/2eM_s)\mathbf{j}$ [11]. β defines the strength of the non-adiabatic interaction, appearing in Eq. (1b), and is expected to be $\sim 10^{-2}$ [8,9]. Adiabatic torque appears in Eq. (1a), with $\eta \equiv 1$ in most models. There are two limiting cases, which occur below and far above breakdown: (I) $\dot{\psi} = 0$ and (II) $\dot{\psi} \gg 1$. The first represents stationary motion wherein $\dot{\mathbf{q}}$ is dictated by Eq. (1b),

$$\dot{\mathbf{q}}_{\text{I}} = (\gamma\Delta/\alpha)H_a + (\beta\mathbf{u})/\alpha. \quad (2)$$

Only the non-adiabatic term drives wall motion. ψ must adapt to maintain equality between Eqs. 1(a and b), and the sole effect of adiabatic torque is to shift the steady-state ψ . Stationary motion exists only up to $\psi = \pi/4$, which occurs at

$$H_W = 2\pi\alpha M_s + (\alpha\eta - \beta)\mathbf{u}/\gamma\Delta. \quad (3)$$

In case (II) the time-average $\langle \sin 2\psi \rangle \rightarrow 0$ in Eq. (1a). Neglecting terms of order α^2 and $\alpha\beta$ with respect to 1,

$$\dot{\mathbf{q}}_{\text{II}} = \gamma \Delta \alpha H_a + \eta \mathbf{u}. \quad (4)$$

In this precessional regime, adiabatic torque alone augments the wall velocity. Adiabatic and nonadiabatic interac-

tions may thus be probed independently by using a field to select regime I or II via Eq. (3). To explore this, wall velocities v were measured in a $20 \text{ nm} \times 600 \text{ nm}$ $\text{Ni}_{80}\text{Fe}_{20}$ nanowire (Fig. 2), using high-bandwidth Kerr polarimetry [12]. The v - H curves of the left wall at $\mathbf{j} = 0$ and $\pm 5.8 \times 10^{11} \text{ A/m}^2$ are linear at low and high H , as expected from Eqs. (2) and (4), and exhibit a peak at $H_W = 6 \text{ Oe}$ marking breakdown. The zero- H data show an anomalous hump at intermediate H , which vanishes with \mathbf{j} and whose cause is currently under investigation. Here we focus on low and high H , where \mathbf{j} simply imparts a vertical shift to $v(H)$. Although Eqs. (2) and (4) predict symmetric shifts about the $\mathbf{j} = 0$ curve, the data show a positive current is more effective at increasing v than a negative current is at decreasing v .

To explore the symmetries of the interaction, $v(\mathbf{j})$ was measured at various constant H , and the symmetric (v_+) and anti-symmetric (v_-) components, $v_{\pm}(\mathbf{j}) = (v(+\mathbf{j}) \pm v(-\mathbf{j}))/2$, were determined. Results at $H = 44 \text{ Oe}$ are shown in Fig. 2. The data reveal a linear component in \mathbf{j} with a nearly constant slope of $\sim 2.7 \times 10^{-7} \text{ m}^3/\text{C}$ over the entire field range studied, and a nonlinear component that is quadratic at low and high H . We interpret the linear component within the model above, and find $\alpha/\beta \approx \eta \approx 1$. However, if the current characteristics are to be interpreted within this 1D model, then likewise must the field characteristics. Eqs. (2) and (4) predict the ratio of the slopes of $v(H)$ above and below breakdown to be α^2 , or $\sim 10^{-4}$, compared to a measured value ~ 0.15 . Adiabatic torque is an analog of the precessional damping that drives wall motion well above breakdown and leads to the high-field mobility. Since the 1D model fails by a factor 10^3 to describe the latter, it is questionable how well it describes the former.

Likewise, Eq. (3) defines a breakdown field dependent on the perpendicular anisotropy and current. We find no more than a $\sim 10\%$ change in H_W over the current range studied, implying $\alpha/\beta \approx \eta$. However, Eq. (3) also predicts a zero- \mathbf{j}

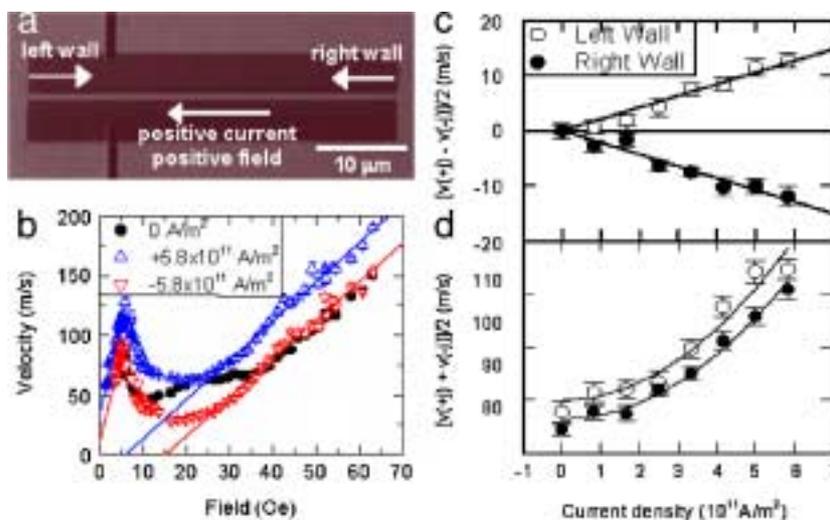


Fig. 2. (a) Plan-view SEM image of nanowire structure. For $\mathbf{j} > 0$ e^- flow to the right, (b) mobility curves of left wall for three currents. (c) Odd and (d) even $v(\mathbf{j})$ components at $H = 44$.

breakdown field of ~ 50 Oe, 10 times larger than the observed 6 Oe, at which the canting angle ψ is only $\sim 4^\circ$. Since the non-adiabatic component is analogous to a field, if the model fails to describe field-driven breakdown by an order of magnitude, it is questionable that variations in H_W can be reliably used to gauge the magnitude of β .

The failure of the 1D model to describe field-driven motion implies that its direct application to current-driven motion may be of limited value. Indeed, no 1D model has predicted the observed nonlinear component in $v(j)$, although its effect can exceed that of the linear component at moderate j . Meaningful comparison between experiment and theory will require models that fully account for realistic, time-variant domain structures, such as the vortex walls known to prevail in many experimental situations [13,14].

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